

# Analysis of the Genealogy Process in Investigative Genetic Genealogy

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Mine Su Erturk

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## PREVIOUS CRIME-SOLVING RESEARCH

### US-VISIT Program

- *PNAS* (2005) and Congressional testimony (2005)
- Led to switch from 2 to 10 fingers

### UIDAI (Aadhaar) Program in India

- *PLOS ONE* (2014) and India Supreme Court briefing (2014)

### Ballistic imaging

- *Journal of Forensic Sciences* 2014, 2017
- *AFTE Journal* 2018 (Stockton CA PD)

### Sexual assault kits

- Testing the backlog: *Journal of Forensic Sciences* 2018  
*cnn.com* 2018
- How to test the backlog: *PNAS* 2020 (SFPD)

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## ACKNOWLEDGMENTS

Colleen Fitzpatrick  
IdentiFinders

Margaret Press  
DNA Doe Project

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## OUTLINE

Introduction: research questions and data  
Main results  
Parameter estimation  
Modeling the two-stage genealogy process  
Proposed strategy  
Limitations  
Conclusions

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## STEPS IN THE IGG PROCESS

1. Obtain DNA sample from crime scene or unidentified remains and perform genotyping (SNPs)

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## STEPS IN THE IGG PROCESS

1. Obtain DNA sample from crime scene or unidentified remains and perform genotyping (SNPs)
2. Upload SNP data to third-party service to obtain relatives of target



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### STEPS IN THE IGG PROCESS

1. Obtain DNA sample from crime scene or unidentified remains and perform genotyping (SNPs)
2. Upload SNP data to third-party service to obtain relatives of target 
- 3. Perform genealogy research to identify target

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### STEPS IN THE IGG PROCESS

1. Obtain DNA sample from crime scene or unidentified remains and perform genotyping (SNPs)
2. Upload SNP data to third-party service to obtain relatives of target 
- 3. Perform genealogy research to identify target
4. Obtain confirmatory DNA sample from identified target or family member

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### RESEARCH QUESTIONS

First mathematical analysis of the **backend** of the IGG process  
(i.e., GEDmatch/FTDNA output → identify target)

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## RESEARCH QUESTIONS

First mathematical analysis of the **backend** of the IGG process  
(i.e., GEDmatch/FTDNA output → identify target)

**Performance analysis:**

Given the GEDmatch/FTDNA output, compute:  
Probability of identifying target  
Expected workload (= size of final family tree)

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## RESEARCH QUESTIONS

First mathematical analysis of the **backend** of the IGG process  
(i.e., GEDmatch/FTDNA output → identify target)

**Performance analysis:**

Given the GEDmatch/FTDNA output, compute:  
Probability of identifying target  
Expected workload (= size of final family tree)

**Optimization:**

How many and which matches to investigate?  
When/if to descend from (possible) **MRCAs**  
(MRCAs = Most Recent Common Ancestor)

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## 17 CASES FROM DNA DOE PROJECT

Case Number $i$	Case Solved $p^i$	Number of Available Matches	Number of Investigated Matches	Number of Identified Matches
1	Yes	2134	31	10
2	No	545	246	25
3	No	4257	50	41
4	No	509	86	22
5	Yes	2000	56	20
6	No	1373	232	171
7	Yes	633	34	29
8	Yes	795	72	68
9	No	928	56	37
10	No	5059	288	212
11	No	5007	39	24
12	Yes	313	107	44
13	Yes	2136	80	66
14	Yes	2417	199	149
15	Yes	308	74	54
16	No	221	31	29
17	No	610	72	43
Total	8	29245	1753	1044

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# GEDmatch OUTPUT

Kir - Jane Doe (Migration - F2 - F)

For Visualization Detail select 1 or more from column 'C'

Kir	Y-DNA	Name	Email	Language	Total cM	Shared	Overlapping	Days Compared	Testing Company
[A]	[A]	[A]	[A]	[A]	14.8	162.3	[A]	2018-01-16	MyHeritage
[A]	[A]	[A]	[A]	[A]	91.8	174.3	[A]	2018-01-14	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.2	97.4	[A]	2018-01-07	23andMe
[A]	[A]	[A]	[A]	[A]	14.1	59.8	[A]	2018-08-11	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.8	64.8	[A]	2018-11-09	MyHeritage
[A]	[A]	[A]	[A]	[A]	21.8	49.3	[A]	2018-01-09	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.2	41.1	[A]	2018-01-08	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.8	44.4	[A]	2018-01-11	23andMe
[A]	[A]	[A]	[A]	[A]	18.8	40.8	[A]	2018-01-27	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.2	40.8	[A]	2018-01-17	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.2	40.8	[A]	2018-01-17	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.8	39.8	[A]	2018-08-16	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.2	37.4	[A]	2018-01-10	23andMe
[A]	[A]	[A]	[A]	[A]	11.8	35.6	[A]	2018-04-11	MyHeritage
[A]	[A]	[A]	[A]	[A]	30.8	35.4	[A]	2018-01-11	MyHeritage
[A]	[A]	[A]	[A]	[A]	15.2	34.2	[A]	2018-01-19	23andMe
[A]	[A]	[A]	[A]	[A]	19.8	32.4	[A]	2018-01-08	MyHeritage
[A]	[A]	[A]	[A]	[A]	17.2	32.4	[A]	2018-01-17	MyHeritage
[A]	[A]	[A]	[A]	[A]	26.2	32.4	[A]	2018-07-23	MyHeritage
[A]	[A]	[A]	[A]	[A]	20.8	32.4	[A]	2018-11-06	MyHeritage
[A]	[A]	[A]	[A]	[A]	20.2	31.4	[A]	2018-01-03	23andMe
[A]	[A]	[A]	[A]	[A]	12.8	31.2	[A]	2018-11-15	23andMe
[A]	[A]	[A]	[A]	[A]	18.8	30.8	[A]	2018-01-16	MyHeritage
[A]	[A]	[A]	[A]	[A]	12.8	30.8	[A]	2018-11-15	23andMe

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Kir - Jane Doe (Migration - F2 - F)

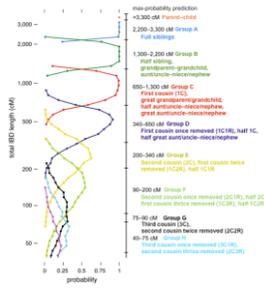
For Visualization Detail select 1 or more from column 'C'

Total cM

Kir	Y-DNA	Name	Email	Language	Total cM	Shared	Overlapping	Days Compared	Testing Company
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# PROBABILISTIC MAPPING FROM TOTAL cM TO RELATIONSHIPS



<https://theadgeek.com/science-the-check-out-of-your-dna-part-3/>  
 Ball et al. (2016), AncestryDNA Matching White Paper.

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## BENCHMARK STRATEGY

Search for MRCAs **between two matches**,  
and immediately descend from these MRCAs

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## BENCHMARK STRATEGY

Search for MRCAs **between two matches**,  
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Investigate **n** matches prioritized by highest total cM

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## BENCHMARK STRATEGY

Search for MRCAs **between two matches**,  
and immediately descend from these MRCAs

Investigate **n** matches prioritized by highest total cM

Vary **n** to generate Pr(identify target) vs. E[workload] curve

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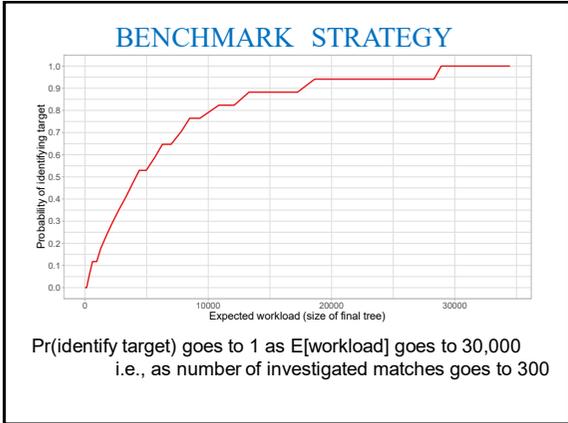
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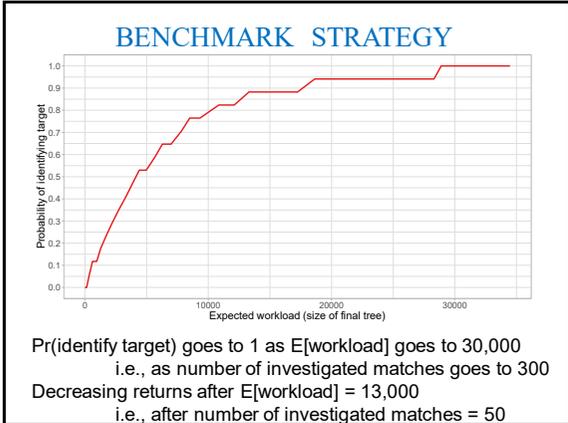
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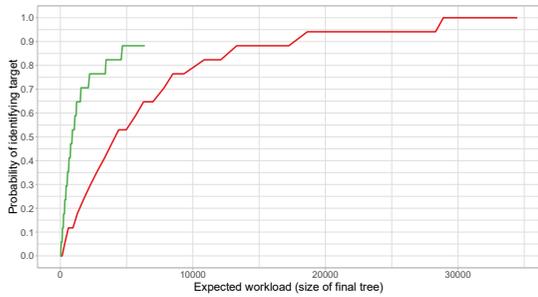
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## PROPOSED vs. BENCHMARK STRATEGY



It solves cases much more quickly: at  $E[\text{workload}] = 2000$ , it solves 71% of cases vs. 27% for Benchmark

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## OUTLINE

Introduction: research questions and data

Main results

➔ Parameter estimation

Modeling the two-stage genealogy process

Proposed strategy

Limitations

Conclusions

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## PARAMETERS

$\Pr(\text{can identify a match}) = 0.59$

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## PARAMETERS

Pr(can identify a match) = 0.59

Pr(can identify someone's spouse) = 1

Pr(can identify someone's child) = 0.98 (also considered 0.90)

Pr(can identify someone's parents) = 0.60 (by simulation)

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## PARAMETERS

Pr(can identify a match) = 0.59

Pr(can identify someone's spouse) = 1

Pr(can identify someone's child) = 0.98 (also considered 0.90)

Pr(can identify someone's parents) = 0.60 (by simulation)

Number of children per couple

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## NUMBER OF CHILDREN PER COUPLE



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## OUTLINE

Introduction: research questions and data

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Parameter estimation

➔ Modeling the two-stage genealogy process

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## ASCENDING STAGE

Given: list of GEDmatch/FTDNA matches to investigate

**Ascending:** build family tree **up** (backwards in time) from matches

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## ASCENDING STAGE

Given: list of GEDmatch/FTDNA matches to investigate

**Ascending:** build family tree **up** (backwards in time) from matches

**Goal:** Find **Most Recent Common Ancestors (MRCAs)** between target and each match

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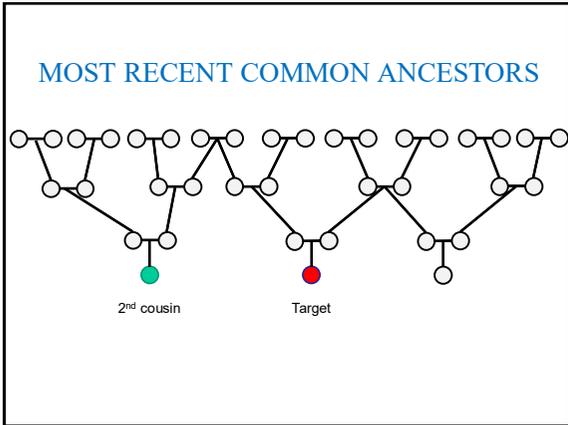
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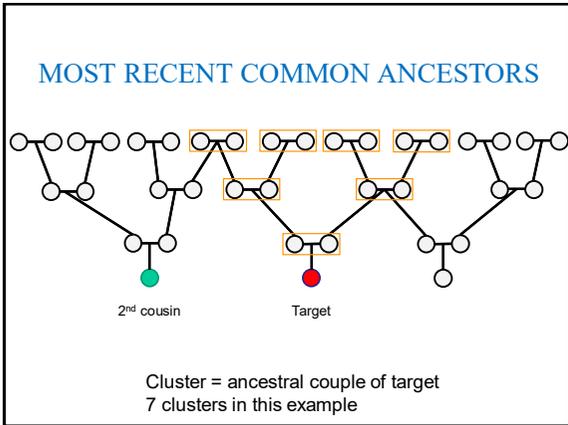
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### ASCENDING STAGE

Given: list of GEDmatch/FTDNA matches to investigate

**Ascending:** build family tree **up** (backwards in time) from matches

**Goal:** Find **Most Recent Common Ancestors (MRCAs)** between target and each match

State of system during ascending stage:  
 For each generation  $g$  and cluster  $c = 1, \dots, 2^{g-1}$   
 $L_{g,c}$  = number of possible MRCAs identified  
 $P_{g,c}$  = Pr(one of the  $L_{g,c}$  MRCAs is the correct MRCA)

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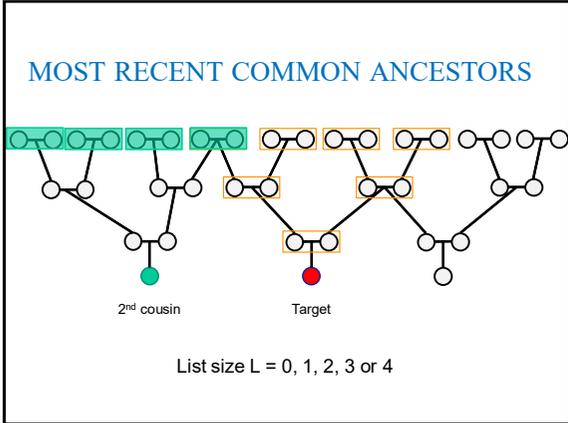
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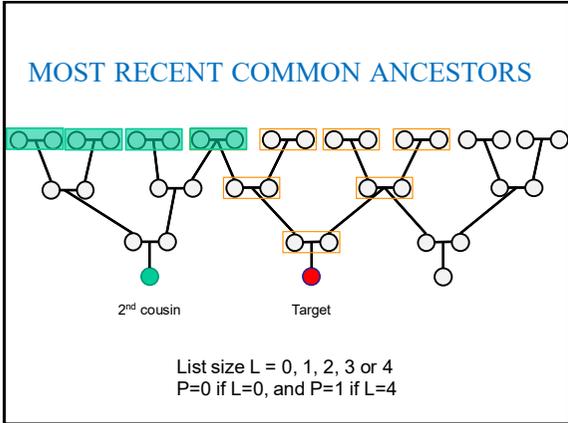
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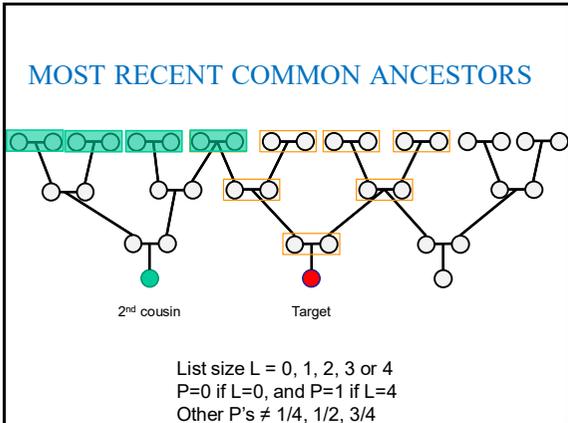
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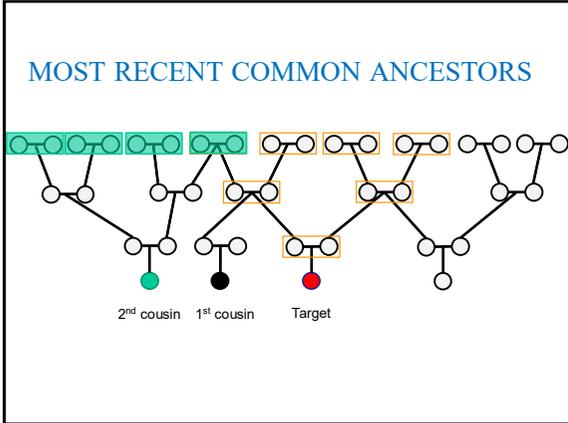
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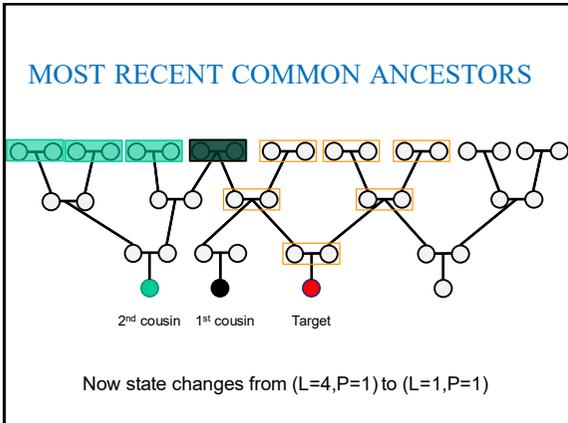
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### DESCENDING STAGE

Given: State of system during ascending stage:  
 For each generation  $g$  and cluster  $c = 1, \dots, 2^{g-1}$   
 $L_{g,c}$  = number of possible MRCA's identified  
 $P_{g,c}$  = Pr(one of the  $L_{g,c}$  MRCA's is the correct MRCA)

**Descending:** build family tree **down** (forwards in time) from possible MRCA's between target and match

**Goal:** Find **intersection** of (i.e., marriage between) maternal and paternal family trees

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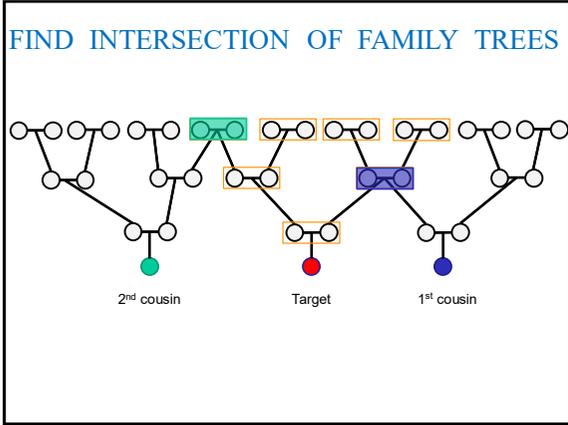
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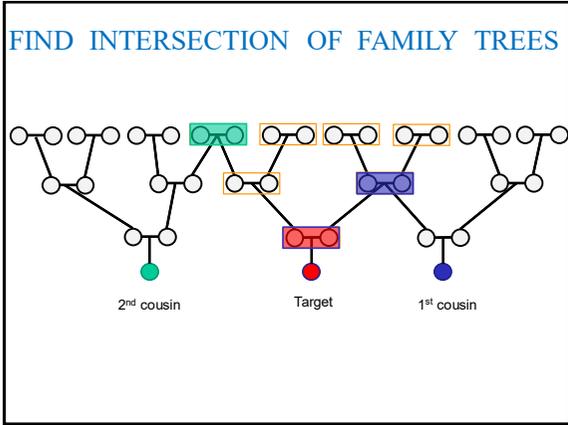
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### DESCENDING STAGE

Given: State of system at end of ascending stage:  
 For each generation  $g$  and cluster  $c = 1, \dots, 2^{g-1}$   
 $L_{g,c}$  = number of possible MRCAs identified  
 $P_{g,c}$  = Pr(one of the  $L_{g,c}$  MRCAs is the correct MRCA)

**Descending:** build family tree **down** (forwards in time) from possible MRCAs between target and match

**Goal:** Find **intersection** of (i.e., marriage between) maternal and paternal family trees

Compute: 1) probability of finding intersection of family trees  
 2) expected workload

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## OUTLINE

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➔ Proposed strategy

Limitations

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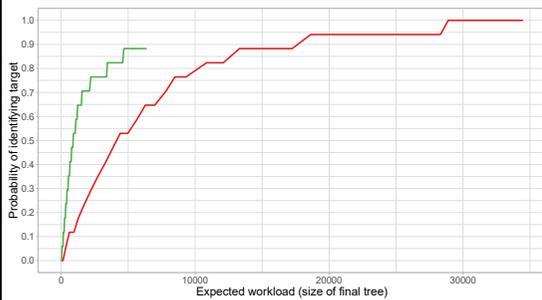
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## PROPOSED vs. BENCHMARK STRATEGY



It solves cases much more quickly: at  $E[\text{workload}] = 2000$ , it solves 71% of cases vs. 27% for Benchmark

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## STOCHASTIC DYNAMIC PROGRAMMING

Observe **state**, take **action**, observe probabilistic transition to new state, take new action,...to maximize **objective**

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## STOCHASTIC DYNAMIC PROGRAMMING

Observe **state**, take **action**, observe probabilistic transition to new state, take new action,...to maximize **objective**

- State:**
- 1) list of uninvestigated matches with cM and cluster
  - 2) for each cluster and generation, Pr(list contains correct MRCA of target) and size of list of MRCAs
  - 3) list of cluster-generation pairs for which a descending search has been performed

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## STOCHASTIC DYNAMIC PROGRAMMING

Observe **state**, take **action**, observe probabilistic transition to new state, take new action,...to maximize **objective**

- State:**
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- Actions:**
- 1) start an ascending search of a new match with cM and cluster
  - 2) start a descending search from cluster-generation
  - 3) end the search

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## STOCHASTIC DYNAMIC PROGRAMMING

Observe **state**, take **action**, observe probabilistic transition to new state, take new action,...to maximize **objective**

- State:**
- 1) list of uninvestigated matches with cM and cluster
  - 2) for each cluster and generation, Pr(list contains correct MRCA of target) and size of list of MRCAs
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- Actions:**
- 1) start an ascending search of a new match with cM and cluster
  - 2) start a descending search from cluster-generation
  - 3) end the search

**Objective:** maximize  $\Pr(\text{target identified}) - (\text{cost} \times E[\text{workload}])$

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**PROPOSED STRATEGY**

SDP problem was too hard to solve (huge state space)

Use a **greedy** (ie, myopic) approach

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**PROPOSED STRATEGY**

SDP problem was too hard to solve (huge state space)

Use a **greedy** (ie, myopic) approach

Given current state:

1) for a descending search, compute  $\Delta P$  (increase in probability of identifying target) and  $\Delta W$  (increase in E[workload]) for each undescended cluster-generation

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SDP problem was too hard to solve (huge state space)

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2) for an ascending search, compute  $\Delta P$  and  $\Delta W$  for each uninvestigated match, assuming that we descend right after ascending

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### PROPOSED STRATEGY

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Use a **greedy** (ie, myopic) approach

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2) for an ascending search, compute  $\Delta P$  and  $\Delta W$  for each uninvestigated match, assuming that we descend right after ascending

3) compute the marginal increase in the objective (ie,  $\Delta P - \text{cost} \times \Delta W$ ) from 1) and 2) and choose the action with the maximum increase (and stop after  $n$  investigations)

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### PROPOSED STRATEGY

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1) for a descending search, compute  $\Delta P$  (increase in probability of identifying target) and  $\Delta W$  (increase in E[workload]) for each undescended cluster-generation

2) for an ascending search, compute  $\Delta P$  and  $\Delta W$  for each uninvestigated match, assuming that we descend right after ascending

3) compute the marginal increase in the objective (ie,  $\Delta P - \text{cost} \times \Delta W$ ) from 1) and 2) and choose the action with the maximum increase (and stop after  $n$  investigations)

Vary  $n$  to generate Pr(target identified) vs. E[workload] curve

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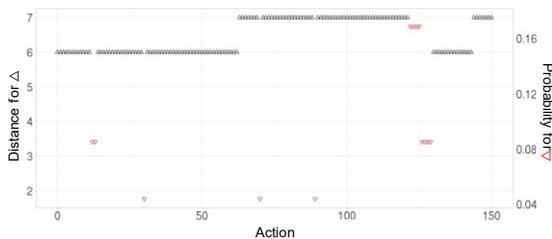
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### PROPOSED STRATEGY FOR CASE #1



Closest matches in Case #1 are at distance 6

$\Delta$  = ascending from distance (left vertical axis)

$\nabla$  = **descending** from cluster-generation with probability of true MRCA (right vertical axis)

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## OUTLINE

Introduction: research questions and data

Main results

Parameter estimation

Modeling the two-stage genealogy process

Proposed strategy

➔ Limitations

Conclusions

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## LIMITATIONS

Cases: small sample size and not chosen randomly

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59

## LIMITATIONS

Cases: small sample size and not chosen randomly

No endogamy

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60

### LIMITATIONS

Cases: small sample size and not chosen randomly

No endogamy

No half-relationships

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61

### LIMITATIONS

Cases: small sample size and not chosen randomly

No endogamy

No half-relationships

No geographical information

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62

### LIMITATIONS

Cases: small sample size and not chosen randomly

No endogamy

No half-relationships

No geographical information

No ethnicity information

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### LIMITATIONS

Cases: small sample size and not chosen randomly

No endogamy

No half-relationships

No geographical information

No ethnicity information

AutoCluster information is perfect

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### LIMITATIONS

Cases: small sample size and not chosen randomly

No endogamy

No half-relationships

No geographical information

No ethnicity information

AutoCluster information is perfect

No Y-STR data to infer surname (Gymrek, *Science* 2013)

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### LIMITATIONS

Cases: small sample size and not chosen randomly

No endogamy

No half-relationships

No geographical information

No ethnicity information

AutoCluster information is perfect

No Y-STR data to infer surname (Gymrek, *Science* 2013)

Search probabilities do not depend on generation

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## OUTLINE

Introduction: research questions and data

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Limitations

➡ Conclusions

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## CONCLUSIONS

$\Pr(\text{identify target})$  and  $E[\text{workload}]$  are **useful only in relative terms**

- But police departments and IGG companies need to assess solvability and workload upfront

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## CONCLUSIONS

$\Pr(\text{identify target})$  and  $E[\text{workload}]$  are **useful only in relative terms**

- But police departments and IGG companies need to assess solvability and workload upfront

Hard cases **appear to be solvable** but require high workload

- Tradeoff curves allow for identification of sweet spot

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## CONCLUSIONS

Pr(identify target) and E[workload] are **useful only in relative terms**

- But police departments and IGG companies need to assess solvability and workload upfront

Hard cases **appear to be solvable** but require high workload

- Tradeoff curves allow for identification of sweet spot

Proposed Strategy solves cases faster by:

- looking for MRCAs **between the target and each match**
- aggressively **descending from possible MRCAs**

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## CONCLUSIONS

Pr(identify target) and E[workload] are **useful only in relative terms**

- But police departments and IGG companies need to assess solvability and workload upfront

Hard cases **appear to be solvable** but require high workload

- Tradeoff curves allow for identification of sweet spot

Proposed Strategy solves cases faster by:

- looking for MRCAs **between the target and each match**
- aggressively **descending from possible MRCAs**

Proposed Strategy is meant to aid, not to replace, genealogists' decisions

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